

2016年B日程第4問



4 $0^\circ \leq \theta \leq 180^\circ$ とする. $15\cos^2\theta - 16\sin\theta\cos\theta - 3 = 0$ のとき, $\tan\theta$ の値は次のようになる.

$$\tan\theta = \boxed{7} \quad (\text{ただし, } 0^\circ \leq \theta \leq 90^\circ)$$

$$\tan\theta = \boxed{8} \quad (\text{ただし, } 90^\circ < \theta \leq 180^\circ)$$

となる.

$$15\cos^2\theta - 16\sin\theta\cos\theta - 3 = 0 \quad \Leftrightarrow \quad 15\cos^2\theta - 16\tan\theta\cos^2\theta - 3 = 0$$

$$1 + \tan^2\theta = \frac{1}{\cos^2\theta} \quad \text{より} \quad \cos^2\theta = \frac{1}{1 + \tan^2\theta}$$

$$\therefore 15 \cdot \frac{1}{1 + \tan^2\theta} - 16\tan\theta \cdot \frac{1}{1 + \tan^2\theta} - 3 = 0$$

$$15 - 16\tan\theta - 3(1 + \tan^2\theta) = 0$$

$$-3\tan^2\theta - 16\tan\theta + 12 = 0$$

$$3\tan^2\theta + 16\tan\theta - 12 = 0$$

$$\therefore (\tan\theta + 6)(3\tan\theta - 2) = 0$$

$$\therefore \left. \begin{array}{l} \tan\theta = \frac{2}{3} \quad (0^\circ \leq \theta \leq 90^\circ \text{ のとき}) \\ \tan\theta = -6 \quad (90^\circ < \theta \leq 180^\circ \text{ のとき}) \end{array} \right\}$$

$$\tan\theta = -6 \quad (90^\circ < \theta \leq 180^\circ \text{ のとき})$$
